



1. Given that

$$\tan \theta^\circ = p, \text{ where } p \text{ is a constant, } p \neq \pm 1$$

use standard trigonometric identities, to find in terms of  $p$ ,

(a)  $\tan 2\theta^\circ$  (2)

(b)  $\cos \theta^\circ$  (2)

(c)  $\cot(\theta - 45)^\circ$  (2)

Write each answer in its simplest form.

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2. Given that

$$f(x) = 2e^x - 5, \quad x \in \mathbb{R}$$

(a) sketch, on separate diagrams, the curve with equation

(i)  $y = f(x)$

(ii)  $y = |f(x)|$

On each diagram, show the coordinates of each point at which the curve meets or cuts the axes.

On each diagram state the equation of the asymptote.

**(6)**

(b) Deduce the set of values of  $x$  for which  $f(x) = |f(x)|$

**(1)**

(c) Find the exact solutions of the equation  $|f(x)| = 2$

**(3)**









3.  $g(\theta) = 4 \cos 2\theta + 2 \sin 2\theta$

Given that  $g(\theta) = R \cos(2\theta - \alpha)$ , where  $R > 0$  and  $0 < \alpha < 90^\circ$ ,

(a) find the exact value of  $R$  and the value of  $\alpha$  to 2 decimal places. (3)

(b) Hence solve, for  $-90^\circ < \theta < 90^\circ$ ,

$$4 \cos 2\theta + 2 \sin 2\theta = 1$$

giving your answers to one decimal place. (5)

Given that  $k$  is a constant and the equation  $g(\theta) = k$  has no solutions,

(c) state the range of possible values of  $k$ . (2)

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**Question 4 continued**

Lined area for writing the answer to Question 4.

**(Total 7 marks)**

Q4



5. The point  $P$  lies on the curve with equation

$$x = (4y - \sin 2y)^2$$

Given that  $P$  has  $(x, y)$  coordinates  $\left(p, \frac{\pi}{2}\right)$ , where  $p$  is a constant,

(a) find the exact value of  $p$ .

**(1)**

The tangent to the curve at  $P$  cuts the  $y$ -axis at the point  $A$ .

(b) Use calculus to find the coordinates of  $A$ .

**(6)**

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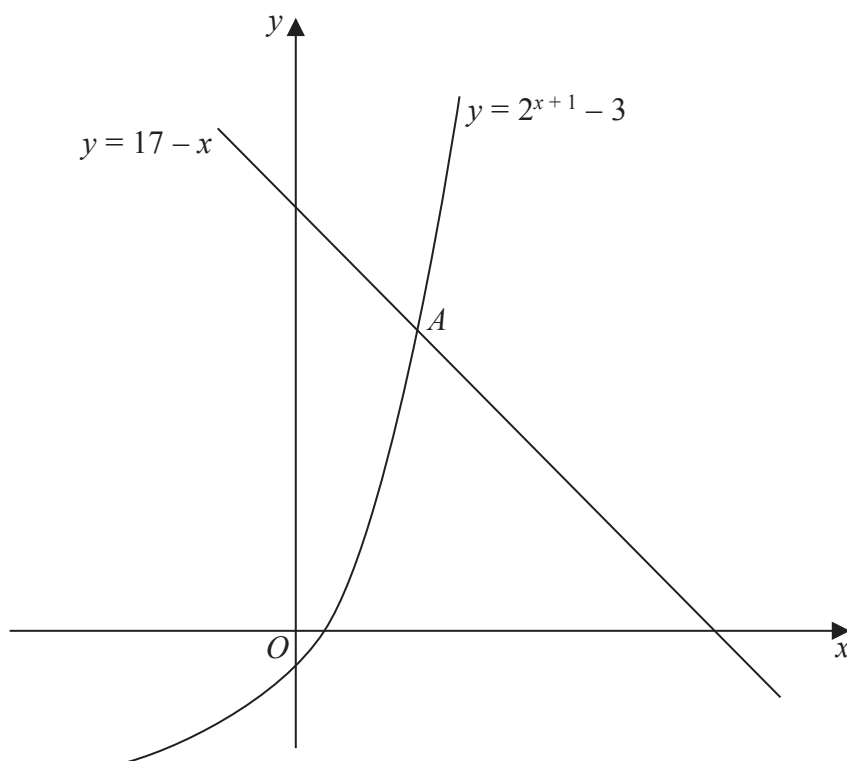








6.



**Figure 1**

Figure 1 is a sketch showing part of the curve with equation  $y = 2^{x+1} - 3$  and part of the line with equation  $y = 17 - x$ .

The curve and the line intersect at the point  $A$ .

(a) Show that the  $x$  coordinate of  $A$  satisfies the equation

$$x = \frac{\ln(20 - x)}{\ln 2} - 1 \quad (3)$$

(b) Use the iterative formula

$$x_{n+1} = \frac{\ln(20 - x_n)}{\ln 2} - 1, \quad x_0 = 3$$

to calculate the values of  $x_1$ ,  $x_2$  and  $x_3$ , giving your answers to 3 decimal places. (3)

(c) Use your answer to part (b) to deduce the coordinates of the point  $A$ , giving your answers to one decimal place. (2)

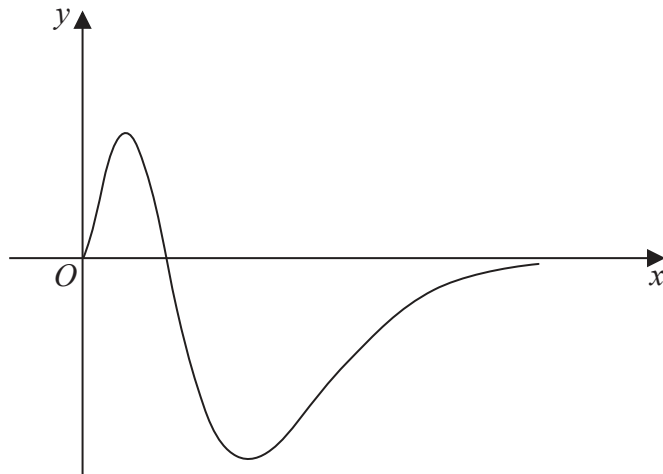








7.



**Figure 2**

Figure 2 shows a sketch of part of the curve with equation

$$g(x) = x^2(1 - x)e^{-2x}, \quad x \geq 0$$

- (a) Show that  $g'(x) = f(x)e^{-2x}$ , where  $f(x)$  is a cubic function to be found. (3)
- (b) Hence find the range of  $g$ . (6)
- (c) State a reason why the function  $g^{-1}(x)$  does not exist. (1)

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**Question 7 continued**

Lined writing area for the answer to Question 7.

Q7

**(Total 10 marks)**



8. (a) Prove that

$$\sec 2A + \tan 2A \equiv \frac{\cos A + \sin A}{\cos A - \sin A}, \quad A \neq \frac{(2n+1)\pi}{4}, \quad n \in \mathbb{Z} \quad (5)$$

(b) Hence solve, for  $0 \leq \theta < 2\pi$ ,

$$\sec 2\theta + \tan 2\theta = \frac{1}{2}$$

Give your answers to 3 decimal places.

(4)

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9. Given that  $k$  is a **negative** constant and that the function  $f(x)$  is defined by

$$f(x) = 2 - \frac{(x - 5k)(x - k)}{x^2 - 3kx + 2k^2}, \quad x \geq 0$$

(a) show that  $f(x) = \frac{x + k}{x - 2k}$  (3)

(b) Hence find  $f'(x)$ , giving your answer in its simplest form. (3)

(c) State, with a reason, whether  $f(x)$  is an increasing or a decreasing function. (2)  
Justify your answer.

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